

Predicting electronic screening for fast Koopmans spectral functionals

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Summary

- Koopmans functionals are powerful orbital-density-dependent functionals that predict spectral properties as accurately as state-of-the-art GW^{1–4}
- they rely on parameters to capture electronic screening
- we construct a ML framework to predict these parameters
- minimal training data is required to achieve desirable accuracy

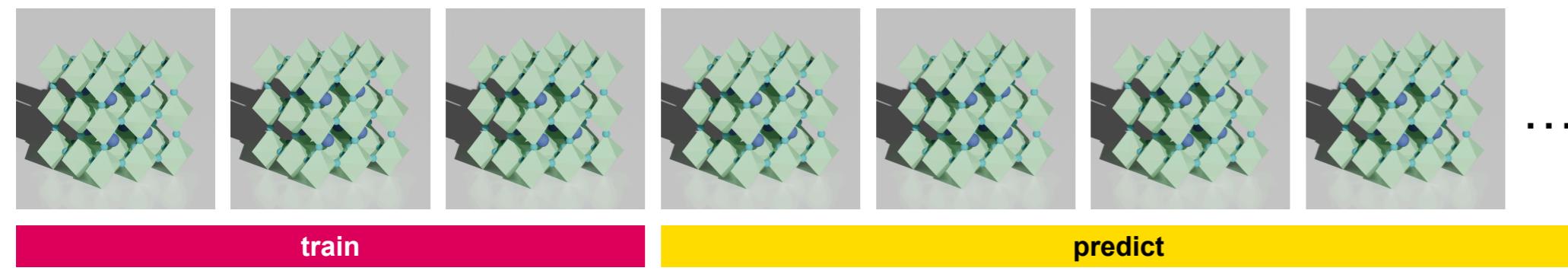
1. What are screening parameters?

$$\alpha_i = \frac{\langle n_i | \varepsilon^{-1} f_{\text{Hxc}} | n_i \rangle}{\langle n_i | f_{\text{Hxc}} | n_i \rangle}$$

- can be computed *ab initio*^{5–7}
- are the vast majority of Koopmans' computational cost
- must be accurate; if $\psi_i(\mathbf{r}) = \sum_j U_{ij} \varphi_j(\mathbf{r})$ then

$$\Delta \varepsilon_{i \in \text{occ}} = \sum_j \alpha_j U_{ij} U_{ji}^\dagger \left(-E_{\text{Hxc}}[\rho - n_j] + E_{\text{Hxc}}[\rho] - \int d\mathbf{r} v_{\text{Hxc}}[\rho](\mathbf{r}) n_j(\mathbf{r}) \right)$$

2. How can machine learning help?



or train on a small cell and deploy on a larger cell (N.B. not a general-purpose model)

3. Our machine learning framework

$$\rho_i(\mathbf{r}) \rightarrow p_{n_1 n_2 l k_1 k_2}^i \rightarrow \alpha_i$$

Descriptors are power spectrum decompositions^{8,9} of orbital densities

$$p_{n_1 n_2 l, k_1 k_2}^i = \pi \sqrt{\frac{8}{2l+1}} \sum_m c_{n_1 l m, k_1}^{i*} c_{n_2 l m, k_2}^i$$

$$c_{nlm,k}^i = \int d\mathbf{r} g_{nl}(r) Y_{lm}(\theta, \varphi) n_i(\mathbf{r} - \mathbf{R}_i)$$

Network is just ridge regression!

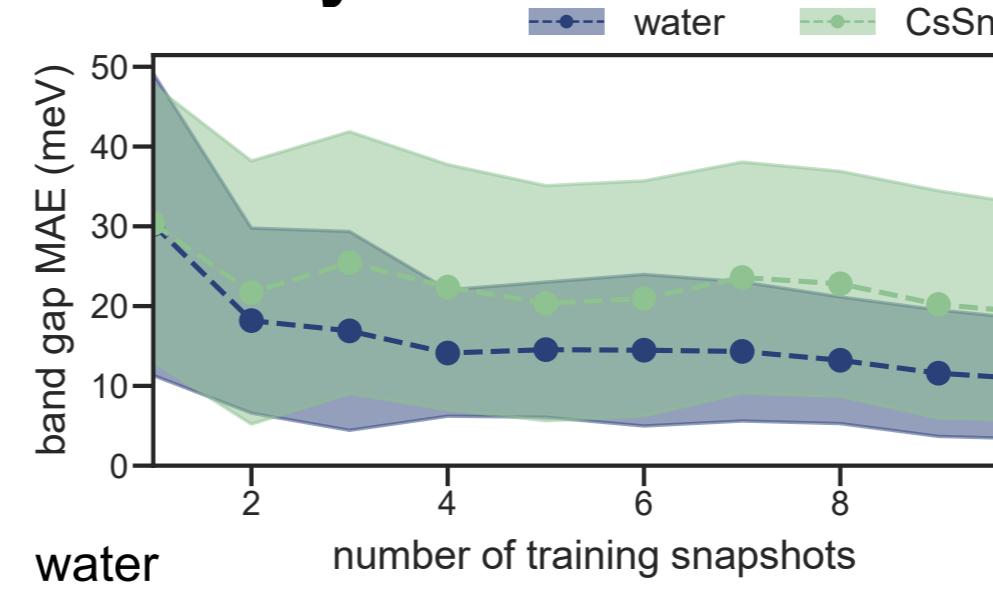
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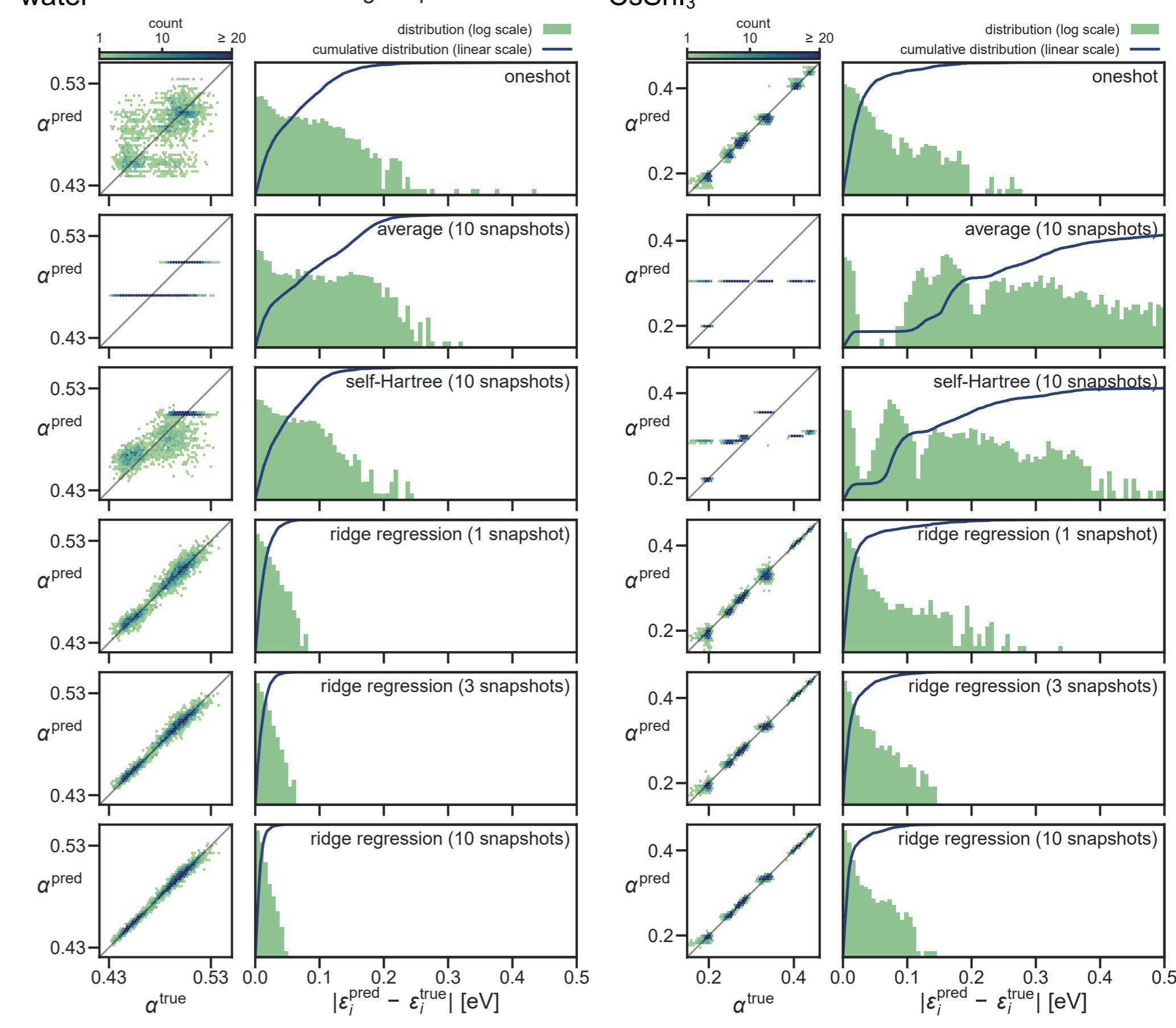
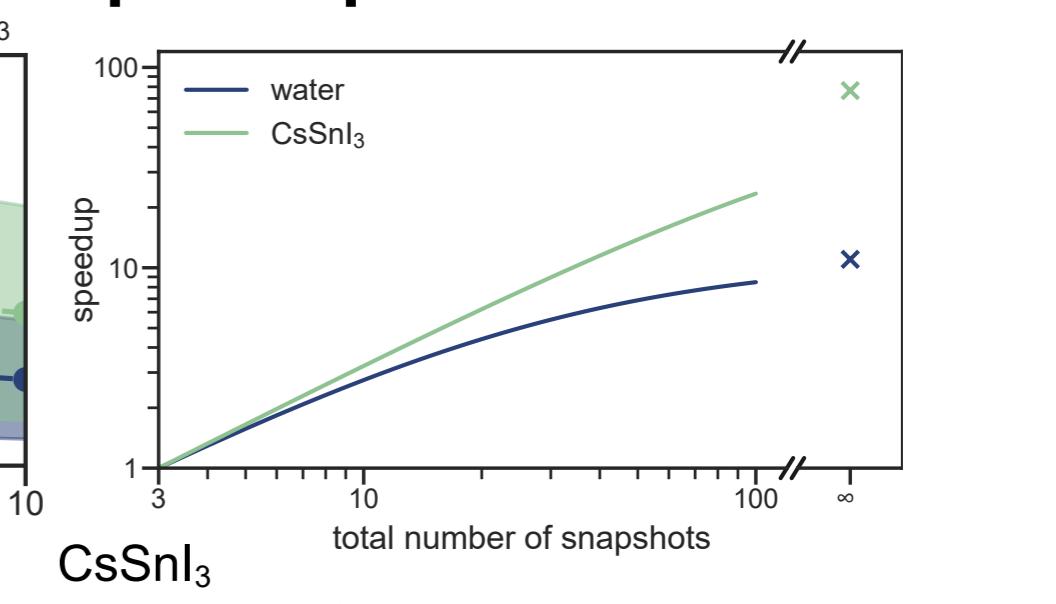
4. Results

- accurate to $\mathcal{O}(10 \text{ meV})$ cf. typical E_g accuracy of $\mathcal{O}(100 \text{ meV})$
- speed-ups from $\mathcal{O}(10)$ to $\mathcal{O}(100)$ times!
- ridge-regression on one snapshot more accurate than oneshot

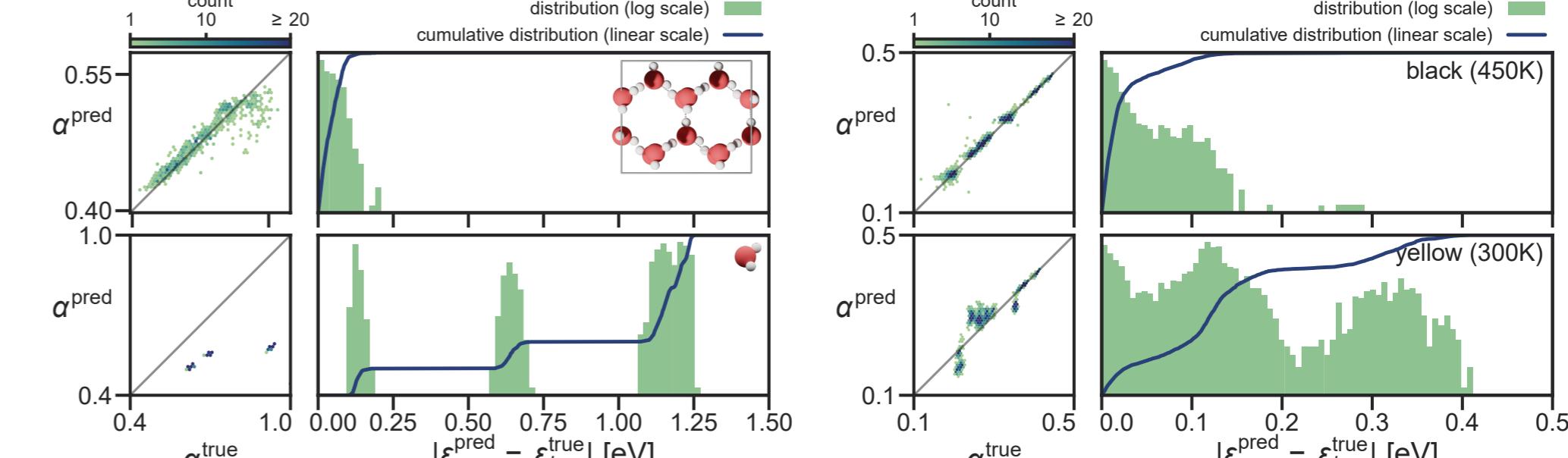
Accuracy



Speed-up



Transferability



5. Takeaways

- lightweight ML can predict Koopmans screening parameters
- more generally, predicting electronic response can be done efficiently with frozen-orbital approximations and ML
- try it now with koopmans! (koopmans-functionals.org)